

Properties of Multiplication

Mathematics is the study of numbers and the laws on how we can use them. These laws are called **properties**. Some of the most important properties are the ones on this anchor chart.

Vocabulary

Zero Property	Any number multiplied by zero has the value of 0. $4 \times 0 = 0$
Identity Property	Any number multiplied by one has the same value. $9 \times 1 = 9$
Commutative Property	The order of a multiplication expression does not change the value. Ex: $4 \times 3 = 3 \times 4$
Distributive Property	A complex multiplication expression can be split into two expressions with one common factor. Ex: $7 \times 6 = (7 \times 5) + (7 \times 1)$
Associative Property	Multiplication expressions with more than two factors can be solved in any order. Ex: $4 \times 6 \times 2 = 4 \times (6 \times 2)$

Zero Property

Any number multiplied by 0 has a value of zero. This is because 0 groups of any number still means 0. Any number of groups with 0 in them still add to 0.

$$0 \times 4 =$$

$$8 \times 0 =$$

Identity Property

Any number multiplied by 1 has the same value.

$$10 \times 1 =$$

$$1 \times 24 =$$

Commutative Property

The order of a multiplication expression does not change its value.

$$4 \times 6 =$$

$$6 \times 4 =$$

Tougher Properties of Multiplication

Two of the more challenging properties of multiplication are the distributive and associative properties. They exist to make multiplication more efficient and accurate.

Distributive Property

A complex multiplication expression can be split into two expressions with one common factor and one split factor.

Shared Common factor - A factor from the original expression that stays the same in the distributive pairs.

Split factor - A factor from the original expression that is decomposed into smaller factors in the distributive pairs.

Example

Split Factors

$$12 \times \underline{4} = (\underline{10} \times \underline{4}) + (\underline{2} \times \underline{4})$$

Shared Common Factors

The diagram shows 12 groups of 2 items (represented by circles with 'xx') on the left. In the center, the equation $12 \times \underline{4} = (\underline{10} \times \underline{4}) + (\underline{2} \times \underline{4})$ is shown. Arrows point from 'Split Factors' to 10 and 2, and from 'Shared Common Factors' to 4. On the right, 10 groups of 2 items and 2 groups of 2 items are shown, representing the decomposition of 12 groups of 2 items.

Associative Property

Multiplication expressions with more than two factors can be solved in any order without changing the product.

Example

$$(6 \times 4) \times 2 = 6 \times (4 \times 2)$$

Solve the given equation and explain what property is shown.

$$7 \times 7 = (_ \times _) + (_ \times _)$$

Solve the given equation and explain what property is shown.

$$14 \times 6 = (_ \times _) + (_ \times _)$$

$$3 \times 12 = (_ \times _) + (_ \times _)$$

$$3 \times 5 \times 2 = \underline{\hspace{2cm}}$$

$$3 \times 6 \times 3 = \underline{\hspace{2cm}}$$

$$21 \times 4 = (_ \times _) + (_ \times _)$$

$$7 \times 2 \times 4 = \underline{\hspace{2cm}}$$

$$4 \times 3 \times 2 = \underline{\hspace{2cm}}$$